# Modeling island effects with probabilistic tier-based strictly local grammars over trees 

Charles Torres ${ }^{1}$, Kenneth Hanson ${ }^{2}$,<br>Thomas Graf ${ }^{3}$, and Connor Mayer ${ }^{4}$<br>${ }^{1,4}$ UC Irvine and ${ }^{2,3}$ Stony Brook University<br>${ }^{1}$ charlt4@uci.edu ${ }^{2}$ kenneth.hanson@stonybrook.edu<br>${ }^{3}$ mail@thomasgraf.net ${ }^{4}$ cjmayer@uci.edu

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## Gradience and Syntactic Formalisms

How does one account for gradience in grammatical acceptability judgments?

Two possibilities:
1 It's not in syntax, so don't worry
2 Extend formalisms to allow for non-discrete judgments

## This work

We investigate using the second strategy with new formalisms from subregular linguistics.

## Collaborators

This is joint work across two institutions: UCI and Stony Brook


Charlie Torres


Kenneth Hanson


Thomas Graf


Connor Mayer

## Outline

1 TSL and $\mathrm{p} T S L$

2 Modeling syntactic dependencies using ( $p$ )TSL over trees

3 Modeling study

4 Modeling study results

## Strictly local languages

SL- $k$ languages are generated by grammars that prohibit certain substrings of length $k$.

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a b c \quad a b c c
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$$
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$$
\begin{array}{ll|lll}
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\end{array}
$$

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\sigma & \ltimes^{k-1}
\end{array}
$$

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$$
G=\{\dot{\sigma} \sigma, \nexists \ltimes\}
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$$

Input: $\rtimes \quad \sigma \quad \sigma^{*} \quad$ б $\ltimes$

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(Albright and Hayes 2003; Daland et al. 2011)


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- Acceptability ratings
(Albright and Hayes 2003; Daland et al. 2011)
- Production frequencies
(Hayes and Londe 2006; Zuraw and Hayes 2017)


## Example: Uyghur backness harmony (simplified)

Description: Vowels in a word must agree in backness

- The vowel /i/ is transparent (relevant later).


## TSL grammar

$G=\{a æ$, æa, wy, $\ldots\}$
$T=\{æ, \mathrm{a}, \varnothing, \mathrm{o}, \mathrm{y}, \mathrm{u}\}$

Data
pæn-lær 'science-PL'
*pæn-lar
at-lar 'horse-PL'
*at-lær

## Gradient blockers

Uvulars are gradient blockers in Uyghur wug tests (Mayer 2021)

Production rates with no uvular:

- pæt-lær (100\%) vs. pæt-lar (0\%)

Production rates with uvular:

- pæq-lær (75\%) vs. pæq-lar (25\%)

Increases tendency for back suffixes, but not categorically!

Does /q/ project?

## String: $\rtimes \quad p$ æ q \| a r $\ltimes$

Does /q/ project?

## Projection 1: $\rtimes$

String: $\rtimes \quad p \quad \nsim \quad q \quad \mid \quad a \quad r \quad \ltimes$

$$
T=\{æ, \mathbf{a}, \varnothing, \mathbf{o}, \mathbf{y}, \mathbf{u}\}
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Does /q/ project?

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Does /q/ project?

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Projection 2: $\rtimes$


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## Does /q/ project?

## Projection 1: <br> $\rtimes$

Projection 2: $\rtimes$


In either case, predicts categorical blocking or failure to block.

## Probabilistic TSL

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Score: Sum of the probabilities of all grammatical projections.

## A simple case

## String: $\rtimes \quad \mathrm{p} \quad æ \quad \mathrm{q} \quad \mid \quad \mathrm{a} \quad \mathrm{r} \quad \ltimes$

$P_{\text {proj }}($ harmonizing vowels $)=1$
$P_{\text {proj }}(\mathrm{q})=0.25$
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$$
1 \times 1 \times .75 \times 1 \times 1 \times 1=0.75
$$

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$P_{\text {proj }}($ harmonizing vowels $)=1$
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Score for /pæqlar/: 0.25

## A more complex case

$\rtimes \quad$ p æ q i q i a r $\quad$ q

## A more complex case



A more complex case


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2 Second, we will see if this can be extended in the same way to handle gradient syntactic judgments.

Preliminaries: Minimalist grammars and movement
Who does Mary think might buy what?

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$$
\text { nom }^{+} \text {nom }^{-}, \text {wh }^{-}
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| $\begin{gathered} \text { does } \\ \mathrm{T}^{+}{ }_{\text {wh }}{ }^{+} \mathrm{C}^{-} \end{gathered}$ |  |
| :---: | :---: |
| $\varepsilon$ | wh-tier |
| $\mathrm{V}^{+}$nom ${ }^{+} \mathrm{T}^{-}$ |  |
| think | does |
| $\mathrm{T}^{+} \mathrm{D}^{+} \mathrm{V}^{-}$ | $\mathrm{T}^{+} \mathrm{wh}^{+} \mathrm{C}^{-}$ |
| Mary might |  |
| $D^{-}\left\{\mathrm{nom}^{-}\right\} \quad \mathrm{V}^{+} \mathrm{nom}^{+} \mathrm{T}^{-}$ | who |
| $\begin{gathered} \stackrel{\prime}{\text { buy }} \\ \mathrm{D}^{+} \stackrel{\mathrm{D}^{+}}{\mathrm{V}^{-}} \end{gathered}$ | $\mathrm{D}^{-}\left\{\mathrm{nom}^{-}, \mathrm{wh}^{-}\right\}$ |
|  |  |
| $D^{-}$\{nom ${ }^{-}$, wh $\left.^{-}\right\} \quad D^{-}$ |  |

## Movement in MGs is tier-based strictly local (TSL)

does


| $\mathrm{T}^{+} \stackrel{\text { does }}{ }{ }^{+} \mathrm{C}^{-}$ |  |
| :---: | :---: |
|  |  |
| $\varepsilon$ | wh-tier |
| $\mathrm{V}^{+}$nom ${ }^{+} \mathrm{T}^{-}$ |  |
| think | does |
| $\mathrm{T}^{+} \mathrm{D}^{+} \mathrm{V}^{-}$ | $\mathrm{T}^{+} \mathrm{wh}^{+} \mathrm{C}^{-}$ |
| Mary might |  |
| $D^{-}\left\{\mathrm{nom}^{-}\right\} \quad \mathrm{V}^{+} \mathrm{nom}{ }^{+} \mathrm{T}^{-}$ | who |
| $\begin{gathered} \text { buy } \\ \mathrm{D}^{+} \mathrm{D}^{+} \mathrm{V}^{-} \end{gathered}$ | $\mathrm{D}^{-}$\{nom ${ }^{-}$, wh $\left.{ }^{-}\right\}$ |
| who what |  |
| $D^{-}\left\{\mathrm{nom}^{-}, \mathrm{wh}^{-}\right\} \quad \mathrm{D}^{-}$ |  |

Feature checking as a constraint on each f-tier
1 Every $\mathrm{f}^{+}$has exactly $1 \mathrm{f}^{-}$among its daughters.
2 Every $f^{-}$has $f^{+}$as its mother.

## Islands as tier blockers

(1) * What did John complain about the fact that Mary brought $\langle$ what $\rangle$ to the party?

```
        did :: T}\mp@subsup{\textrm{T}}{}{+}\mp@subsup{\textrm{wh}}{}{+}\mp@subsup{\textrm{C}}{}{-
        \varepsilon:: \mp@subsup{V}{}{+}}\mp@subsup{\textrm{nom}}{}{+}\mp@subsup{\textrm{T}}{}{-
        complain :: P}\mp@subsup{\textrm{P}}{}{+}\mp@subsup{\textrm{D}}{}{+}\mp@subsup{\textrm{V}}{}{-
    John :: D}\overline{\mp@subsup{D}{}{-}{\mp@subsup{\mathrm{ nom }}{}{-}} about :: D}\mp@subsup{\textrm{D}}{}{+}\mp@subsup{\textrm{P}}{}{-
        the :: N+}\mp@subsup{\textrm{N}}{}{+
        fact :: C}\mp@subsup{\textrm{C}}{}{+}\mp@subsup{\textrm{N}}{}{-
        that :: T T+}\mp@subsup{\textrm{C}}{}{-
        \varepsilon:: \mp@subsup{V}{}{+}}\mp@subsup{\textrm{nom}}{}{+}\mp@subsup{\textrm{T}}{}{-
    brought :: P}\mp@subsup{}{}{+}\mp@subsup{\textrm{D}}{}{+}\mp@subsup{\textrm{D}}{}{+}\mp@subsup{\textrm{V}}{}{-
```



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```
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        \varepsilon:: \mp@subsup{V}{}{+}}\mp@subsup{\textrm{nom}}{}{+}\mp@subsup{\textrm{T}}{}{-
    complain :: P}\mp@subsup{\textrm{P}}{}{+}\mp@subsup{\textrm{D}}{}{+}\mp@subsup{\textrm{V}}{}{-
```



```
        the :: N+}\mp@subsup{}{}{+}\mp@subsup{D}{}{-
        fact :: C+}\mp@subsup{\textrm{N}}{}{-
        that :: T T+}\mp@subsup{\textrm{C}}{}{-
        \varepsilon:: V }\mp@subsup{}{}{+}\mp@subsup{\textrm{nom}}{}{+}\mp@subsup{\textrm{T}}{}{-
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```



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```
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        \varepsilon:: \mp@subsup{V}{}{+}}\mp@subsup{\textrm{nom}}{}{+}\mp@subsup{\textrm{T}}{}{-
    complain :: P}\mp@subsup{\textrm{P}}{}{+}\mp@subsup{\textrm{D}}{}{+}\mp@subsup{\textrm{V}}{}{-
    John :: D
        the :: N+}\mp@subsup{}{}{+}\mp@subsup{D}{}{-
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```



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$$
\begin{aligned}
& \text { did :: } \mathrm{T}^{+}{ }^{\mathrm{wh}}{ }^{+} \mathrm{C}^{-} \\
& \varepsilon:: \mathrm{V}^{+} \mathrm{nom}^{+} \mathrm{T}^{-} \\
& \text {complain :: } \mathrm{P}^{+} \mathrm{D}^{+} \mathrm{V}^{-} \\
& \text {John :: } \mathrm{D}^{-}\left\{\text {nom }^{-}\right\} \quad \text { about :: } \mathrm{D}^{+} \mathrm{P}^{-} \\
& \text {the :: } \mathrm{N}^{+} \mathrm{D}^{-} \\
& \text {fact :: } \mathrm{C}^{+} \mathrm{N}^{-} \\
& \text {that :: } \mathrm{T}^{+} \mathrm{C}^{-} \\
& \varepsilon:: \mathrm{V}^{+} \mathrm{nom}^{+} \mathrm{T}^{-} \\
& \text {brought :: } \mathrm{P}^{+} \mathrm{D}^{+} \mathrm{D}^{+} \mathrm{V}^{-} \\
& \text {Mary :: } \mathrm{D}^{-}\left\{\text {nom }^{-}\right\} \text {what :: } \mathrm{D}^{-}\left\{\mathrm{wh}^{-}\right\} \text {to the party :: } \mathrm{P}^{-}
\end{aligned}
$$

## Probabilistic tree projection

- $P_{p r o j}($ fact $)=0.7$
- $P_{\text {proj }}=1$ for all wh nodes, 0 otherwise


Mary :: $\left.\overline{D^{-}\{\text {nom }}{ }^{-}\right\} \quad$ what :: $D^{-}\left\{\mathrm{wh}^{-}\right\} \quad$ to the party :: $\mathrm{P}^{-}$

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|  |  |
| :---: | :---: |
| $\begin{aligned} & \text { did :: } \mathrm{T}^{+} \mathrm{mh}^{+} \mathrm{C}^{-} \\ & \varepsilon:: \mathrm{v}^{+} \mathrm{nom}^{+} \mathrm{T}^{-} \end{aligned}$ <br> complain :: $\mathrm{P}^{+} \mathrm{D}^{+} \mathrm{V}^{-}$ | Fact doesn't project <br> did :: $\mathrm{T}^{+}{ }^{\mathrm{wh}}{ }^{+} \mathrm{C}^{-}$ <br> what :: $\mathrm{D}^{-}\left\{\mathrm{wh}^{-}\right\}$ |
|  |  |
| $\varepsilon:: \mathrm{v}^{+} \mathrm{nom}^{+} \mathrm{T}^{-}$ |  |
| brought :: $\mathrm{P}^{+} \mathrm{D}^{+} \mathrm{D}^{+} \mathrm{v}^{-}$ |  |

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## Modeling Island Effects using pTSL over Trees

Remainder of this talk: a modeling study that captures gradient island effects in experimental acceptability judgments.

Fit $P_{\text {proj }}$ to English experimental data from Sprouse et al. (2016).


Figure: Jon Sprouse

## The Sprouse data

The Sprouse data are sentences balanced for two factors:

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- Matrix or embedded clause extraction.

Example:
(2) a. Who $t$ thinks [that John bought a car]? (non-island, matrix clause)
b. What do you think [that John bought $t$ ? (non-island, embedded clause)
c. Who $t$ wonders [whether John bought a car]? (island, matrix clause)
d. What do you wonder [whether John bought $t$ ]? (island, embedded)

## The Sprouse data

Only sentences with extraction from an embedded clause over an island structure should be ungrammatical.

- Superadditivity: effect of these two factors together is greater than their individual effects.



## Island types

We restricted ourselves to three subsets of island effects:
1 Whether islands: *What do you wonder whether John bought $t$ ?
2 Complex NP islands: *Who did Mary deny the rumor that John likes $t$ ?

3 Adjunct islands: *Who did Mary complain because John likes $t$ ?

The Complex NP Constraint and Adjunct Island Constraint also apply to extraction out of relative clauses.

- We treat both as involving wh features for simplicity.


## Adapting the data

Each of these sentences has a Likert score assigned by the participants.

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We converted each sentence in the data set into dependency tree format.

## Fitting the model

Some projection probabilities set a priori:

- Most nodes set to 0
- wh nodes set to 1

Free parameters: Blockers in the discrete analysis.

- that $:: \mathrm{T}^{+} \mathrm{C}^{-}$(whether/adjunct islands)
- whether :: $\mathrm{T}^{+} \mathrm{C}^{-}$(whether/adjunct islands)
- if :: $\mathrm{T}^{+} \mathrm{C}^{-}$(whether/adjunct islands)
- all nodes whose feature annotation contains the substring $\mathrm{C}^{+} \mathrm{N}^{-}$(complex NP islands)


## Fitting the model

Free parameters fit to data set consisting of dependency trees with mean normalized Likert ratings.

Model assigns values in $[0,1]$ to each tree.

We find projection probabilities that minimize the mean squared error between model and human scores.

## Super-additivity: Humans vs. pTSL



Figure: Super-additivity in a pTSL model

## Fit Projection Probabilities

| Node | Projection probability |
| :--- | ---: |
| that $:: \mathrm{T}^{+} \mathrm{C}^{-}$ | .46 |
| $\mathrm{C}^{+} \mathrm{N}^{-}$ | .63 |
| whether $:: \mathrm{T}^{+} \mathrm{C}^{-}$ | .73 |
| if :: $\mathrm{T}^{+} \mathrm{C}^{-}$ | .89 |
| Table: Fit projection probabilities |  |

Higher probability means greater propensity to block and induce island effects.

## Discussion

The model succeeds in some respects:

- Captures supperadditivity
- Relative badness of different types of islands.

The model fails in other respects:

- Overpredicts superadditivity in some cases
- Doesn't account for variability in non-island cases.


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Some of the probabilities likely encode non-syntactic features:

- 'that' isn't typically considered a blocker.
- Encodes (non-syntactic?) decrease in acceptability between matrix and embedded extraction.


## Takeaways

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- The same computational structure can be applied to constraints in phonology and in syntax.
- pTSL over trees can capture superadditivity and gradience in syntactic island effects.


## Take-home message

pTSL over trees lets us model gradience arising from grammatical factors.

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whether island


## Adjunct island



